

# 模拟与数字电路

## Analog and Digital Circuits



课程主页 扫一扫

第八讲：竞争与时序逻辑 电路

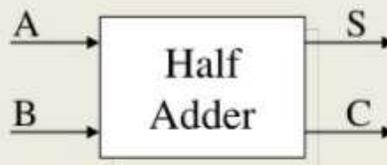
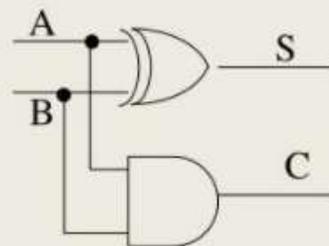
Lecture 8: Hazards and Sequential logics

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# 提纲

- 复习
  - 右图是一个半加器的Verilog
  - 试判断下图的模块的逻辑模块
- 竞争、冒险、毛刺
- 时序电路
- 锁存器



```
module half_adder(S, C, A, B);
output S, C;
input A, B;

wire S, C, A, B;

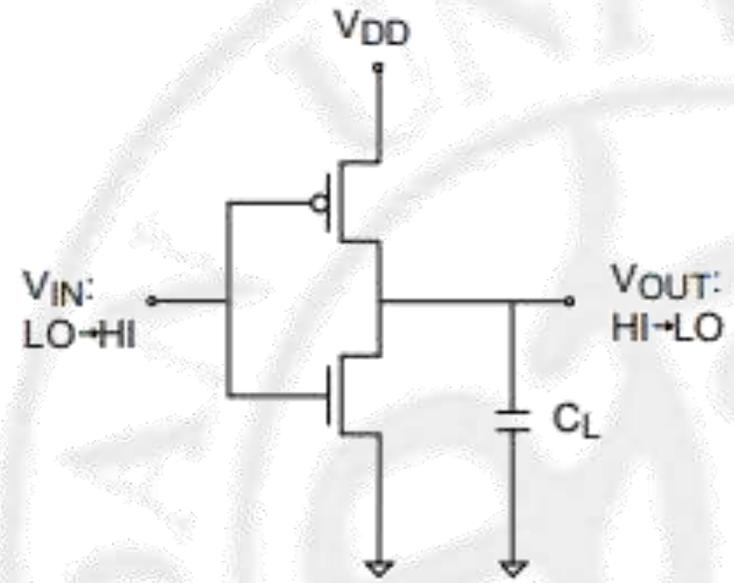
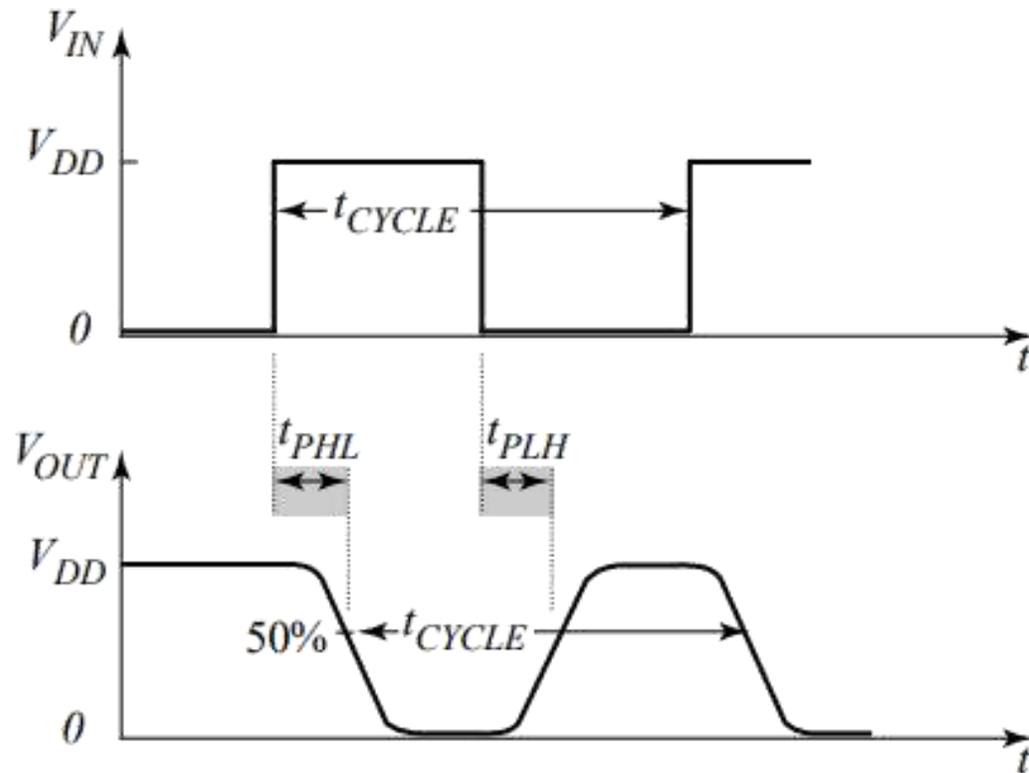
assign S = A ^ B;
assign C = A & B;

endmodule
```

```
module XYZ (S,C,x,y,z);
input x,y,z;
output S,C;
wire S1,D1,D2; //Outputs of first XOR and two AND gates
//Instantiate the halfadder
halfadder HA1 (S1,D1,x,y),
            HA2 (S,D2,S1,z);
or g1(C,D2,D1);
endmodule
```

# 逻辑门延时

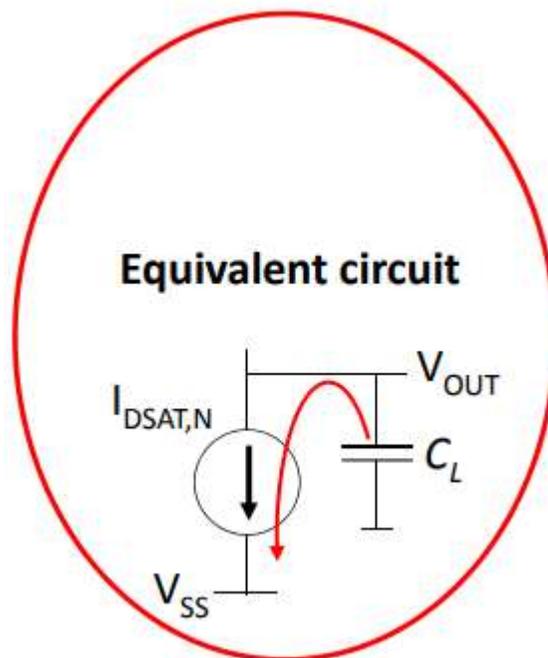
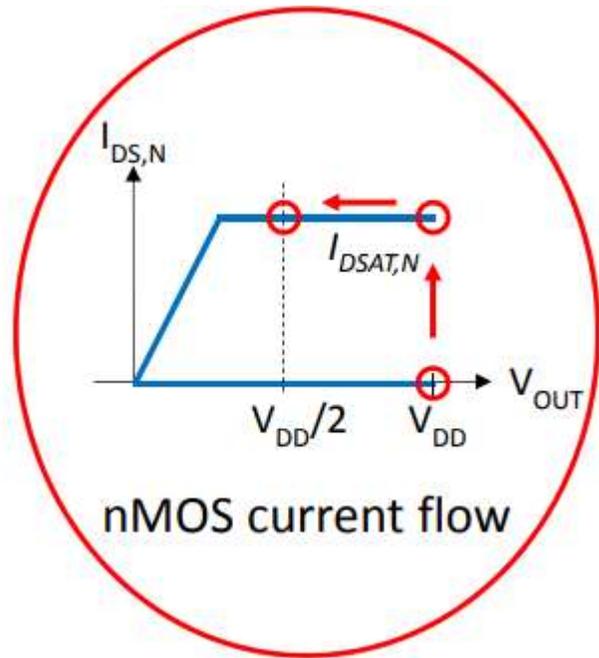
- 实际逻辑门存在延时



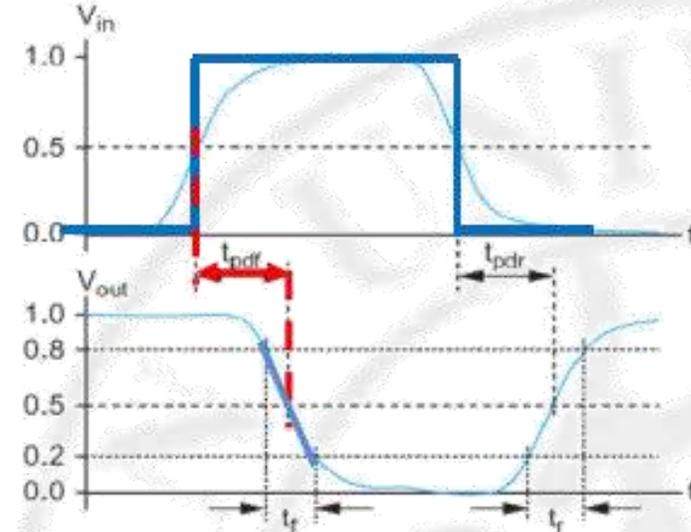
以反相器为例：延时是负载电容漏电、放电的过程

# 反相器延时

- 反相器输入从低到高
  - 先进工艺下，反相器延时约在10ps



## Square wave approximation

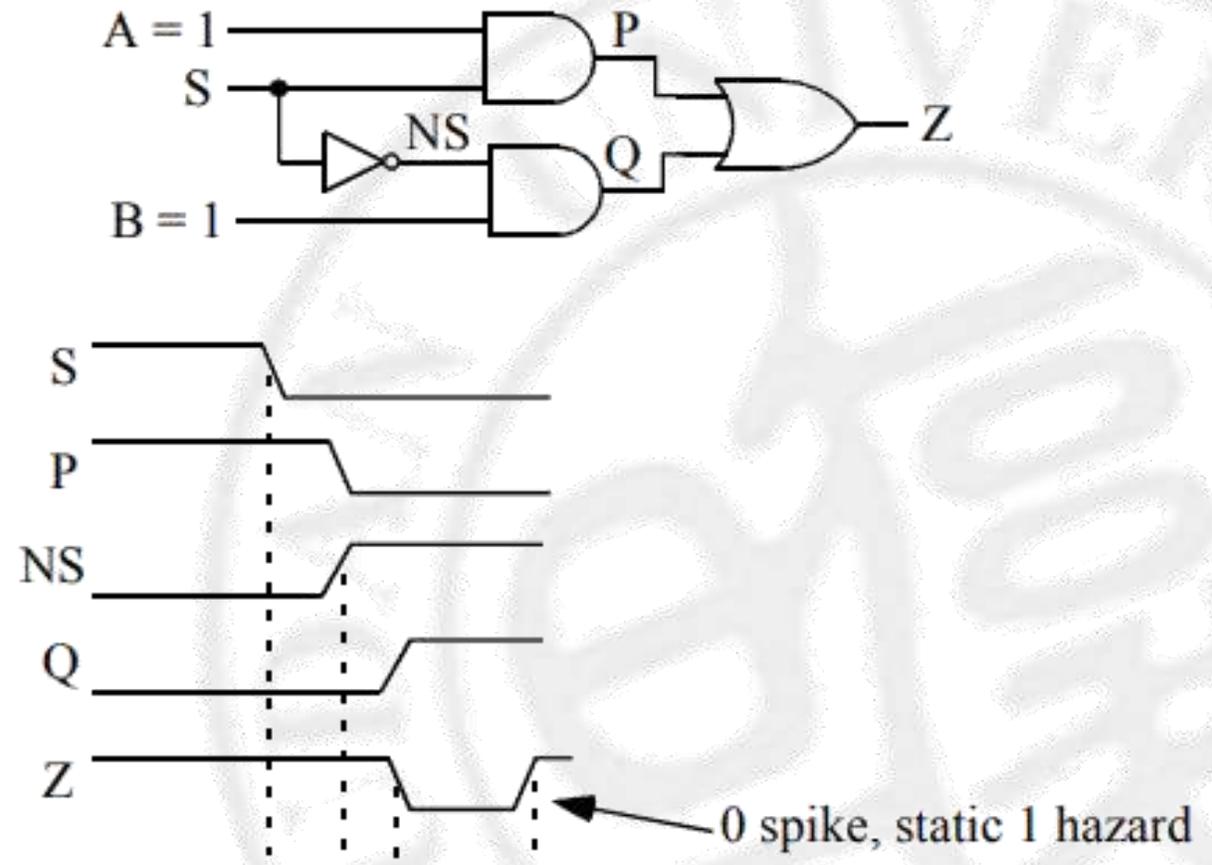


$$t_{pdr} = \frac{\Delta Q}{I_{DSAT,N}} = \frac{C_L \cdot \Delta V_{OUT}}{I_{DSAT,N}}$$

$$\Delta V_{OUT} = V_{DD}/2$$

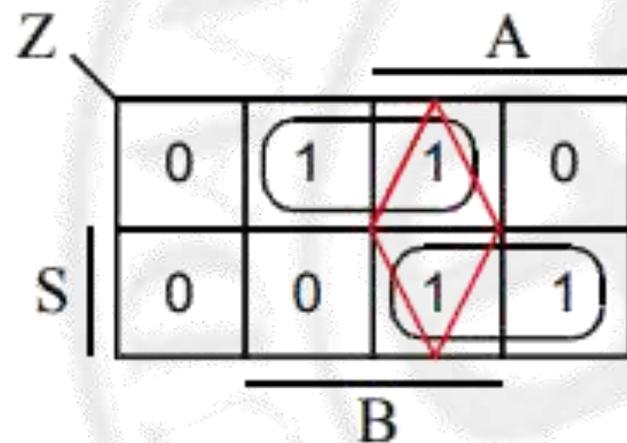
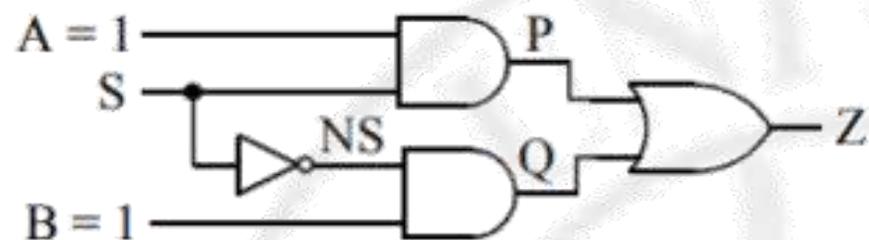
# Timing Hazards 竞争冒险

- 假设下列电路中的逻辑门具有相同的延时，在右图逻辑中：输入A/B保持不变，S从高到低，画出Z的时序波形。

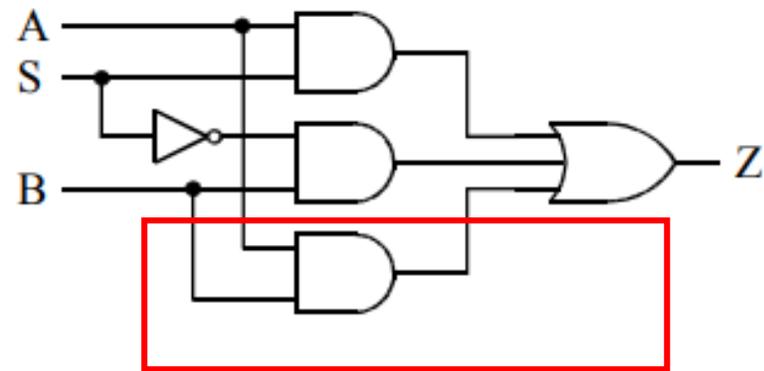
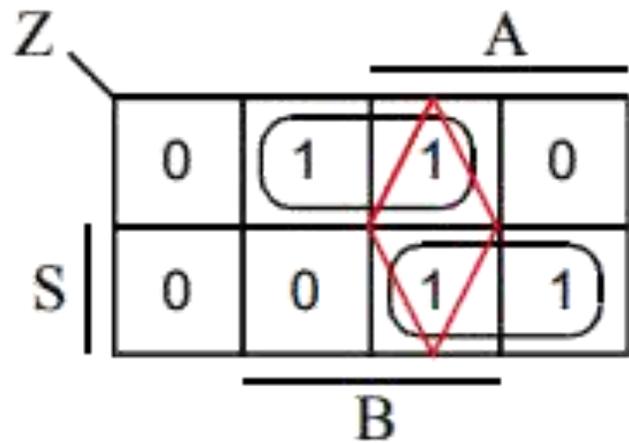
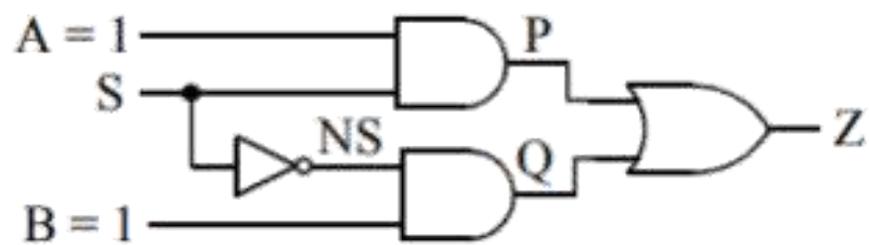


# 基于卡诺图的Hazard推断

- Hazard原因：逻辑延时差
- 存在两个AND，其中一个AND门前没有非门，另一个前有非门
- 卡诺图上，相邻的格子均为1，但是，并未被同一个圈包裹



# Hazard解决方案（一）：冗余项

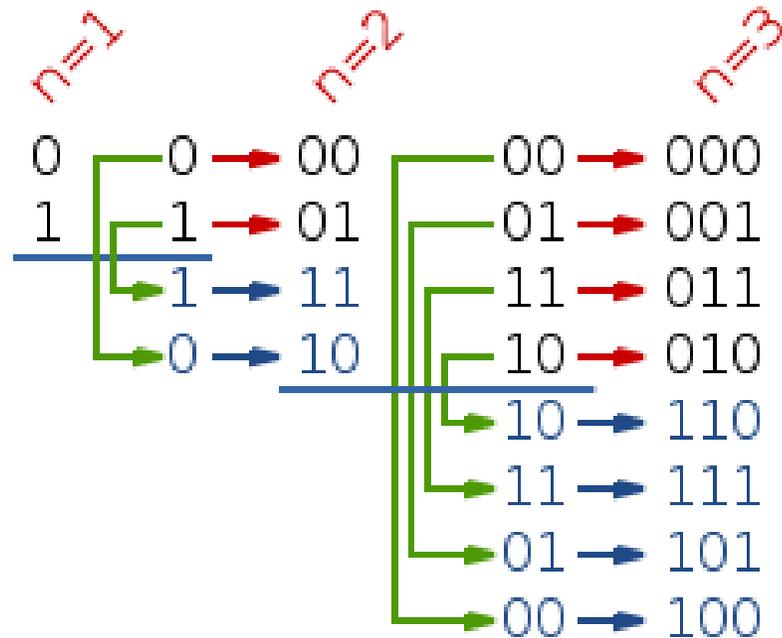


补充冗余项：将红色格子代表的门再次加回

# Hazard解决方案（二）：专用编码

- 格雷码 Gray Code

- 特点计数变化时，每次仅有1位变化



Decimal Number	4 bit Binary Number ABCD	4 bit Gray Code G <sub>1</sub> G <sub>2</sub> G <sub>3</sub> G <sub>4</sub>
0	0000	0000
1	0001	0001
2	0010	0011
3	0011	0010
4	0100	0110
5	0101	0111
6	0110	0101
7	0111	0100
8	1000	1100
9	1001	1101
10	1010	1111
11	1011	1110
12	1100	1010
13	1101	1011
14	1110	1001
15	1111	1000

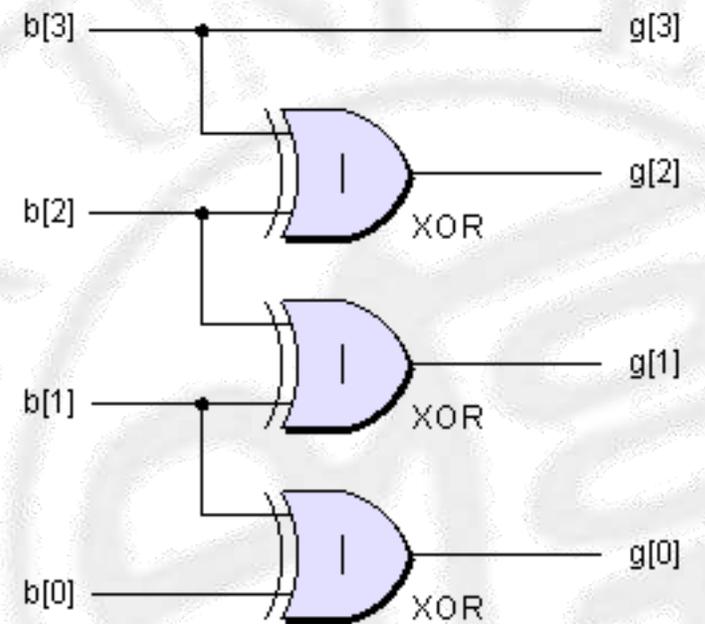
# Hazard解决方案（二）：专用编码

- 格雷码的硬件实现（卡诺图）

$b_3b_2$ \ $b_1b_0$	00	01	11	10
00	0	1	0	1
01	0	1	0	1
11	0	1	0	1
10	0	1	0	1

$b_3b_2$ \ $b_1b_0$	00	01	11	10
00	0	0	0	0
01	1	1	1	1
11	0	0	0	0
10	1	1	1	1

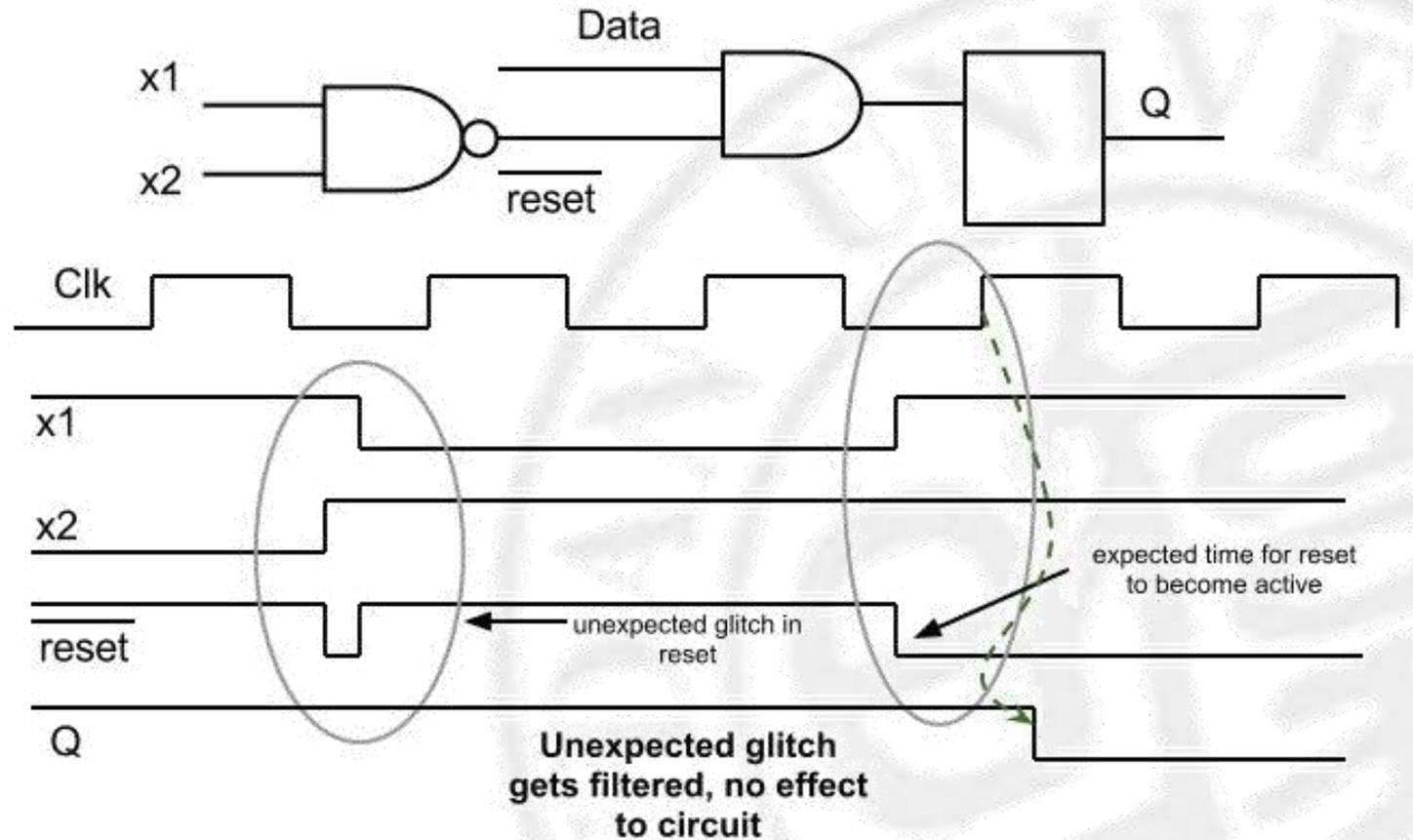
$b_3b_2$ \ $b_1b_0$	00	01	11	10
00	0	0	1	1
01	1	1	0	0
11	1	1	0	0
10	0	0	1	1



# Hazard补偿方法（三）：同步时序电路

- 举例

- 考试过程中的某个瞬间对错不在乎
- 只关心交卷状态的成绩



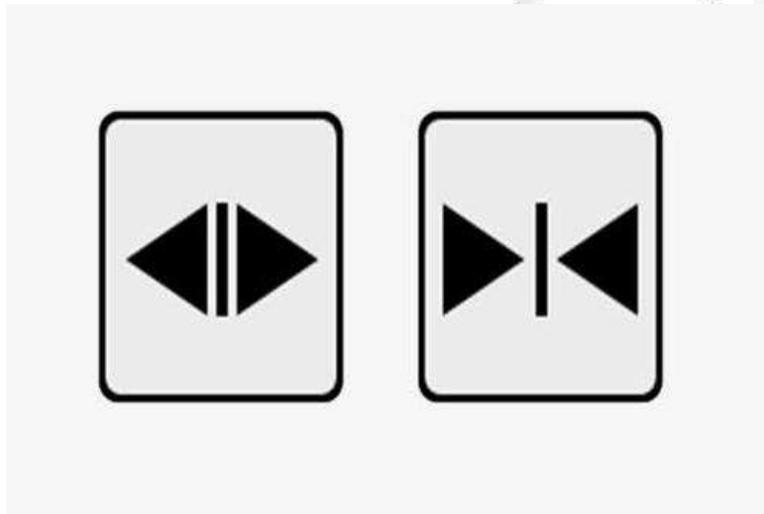
同步电路采用时钟才采样某个有效瞬间

# 时序逻辑 vs 组合逻辑

- 同步电路并不是组合逻辑，他存在一个器件使得

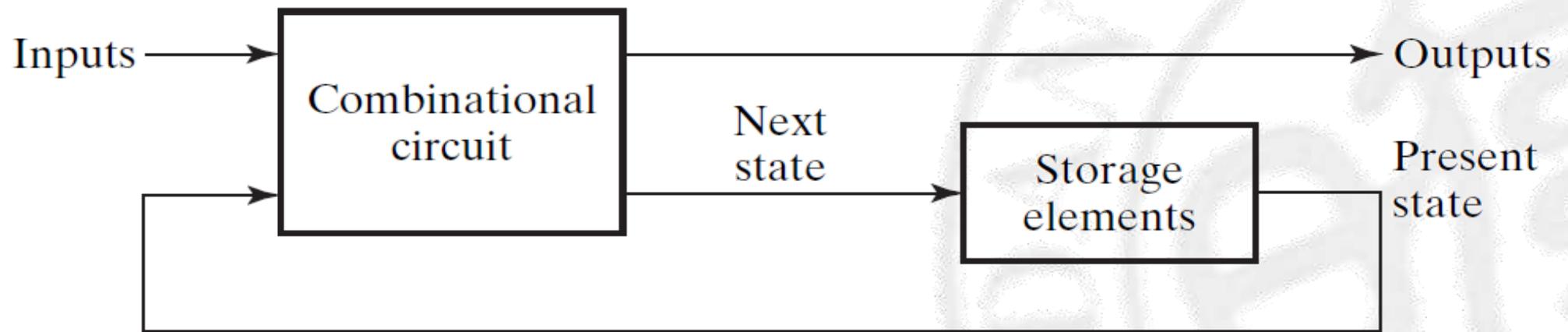
输出不仅跟当前的输入有关，而且**跟过去的输入也有关**。这就要求在电路中必须包含一些**存储元件**来记住这些输入的过去值。

- 生活中的时序逻辑  
举例：电梯开关门



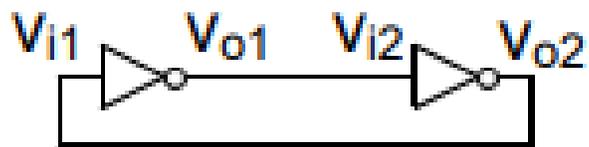
# 时序电路

- 组合逻辑+存储单元
- 输入和输出基于之前的状态与目前状态

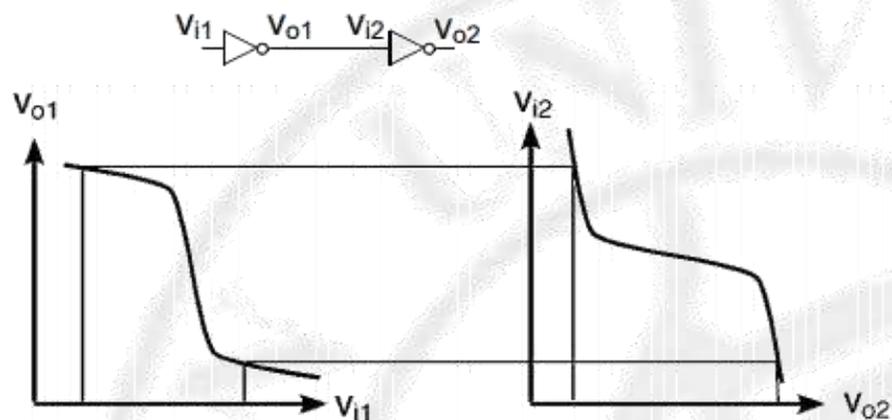


# 基于正反馈的存储单元

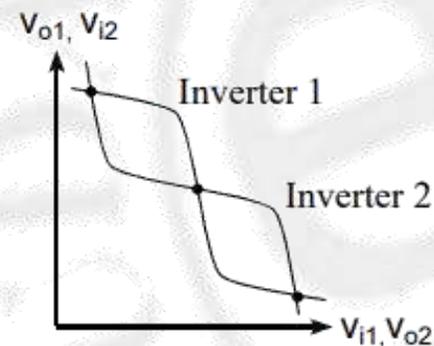
Latch可等效为反相器的级联  
存在2-3个解  
其中有一个是亚稳态



- Now consider the behavior of the following circuit:



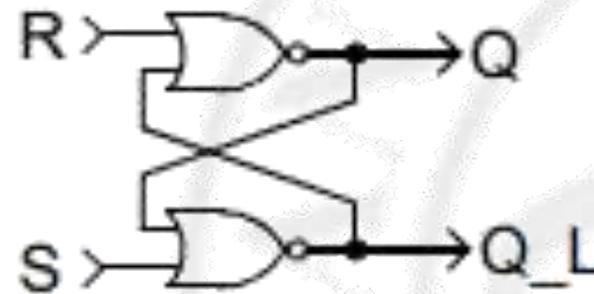
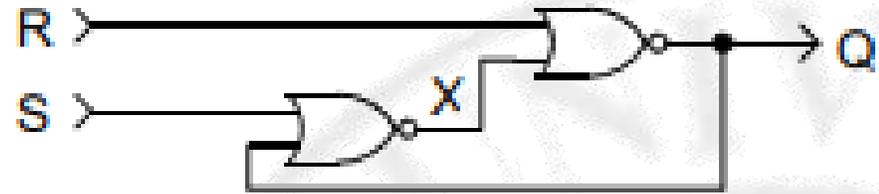
- Superimposing the two graphs gives the following:



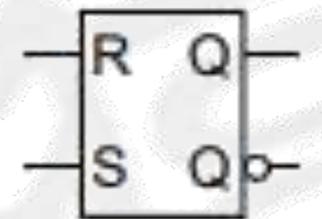
# 时序电路 基础原件：SR锁存器

- 假设开关门逻辑存在两个输入：  
Set（关门） / Reset（开门）
- 上述电路的真值表如下：

INPUTS		OUTPUT	STATE
S	R	Q	
0	0	No Change	Previous
0	1	0	Reset
1	0	1	Set
1	1	-	Forbidden



Logic Diagram

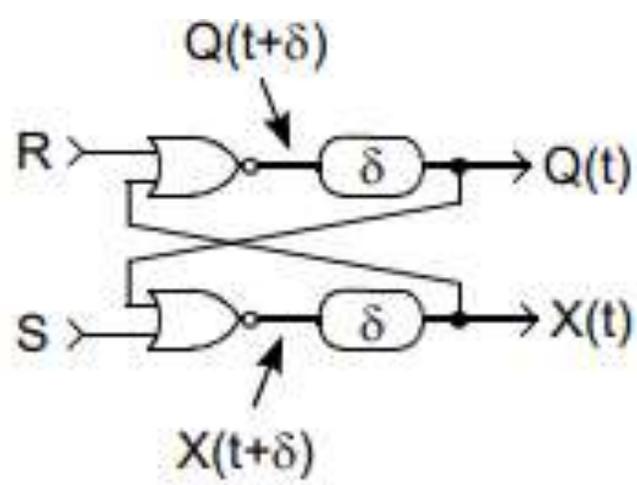
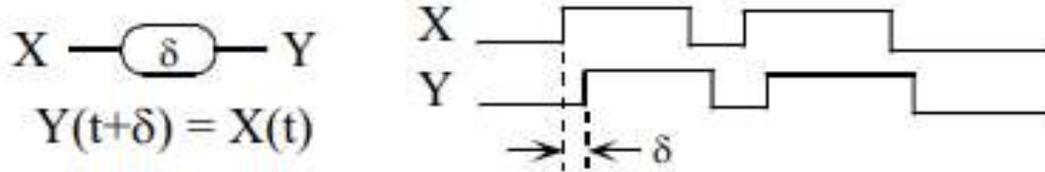


Symbol

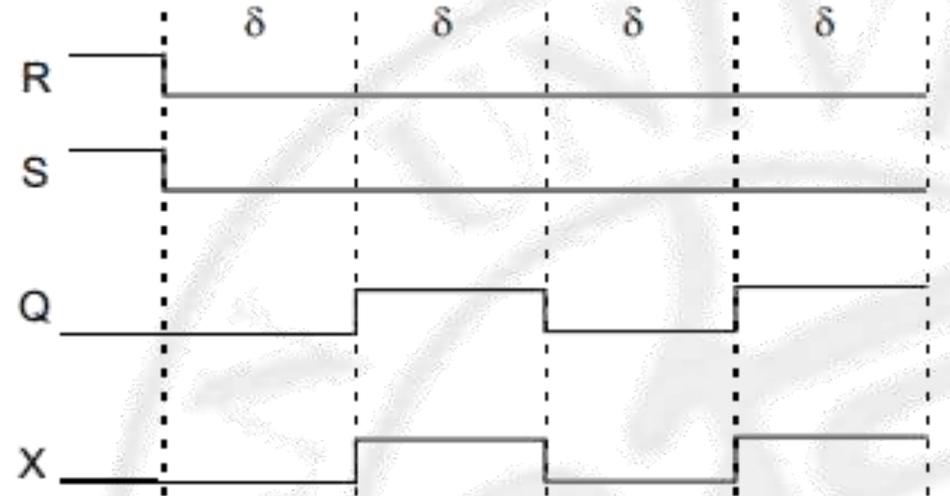
SR 锁存器

# 锁存器的非稳态实现

- 假设逻辑门存在延时  $\delta$

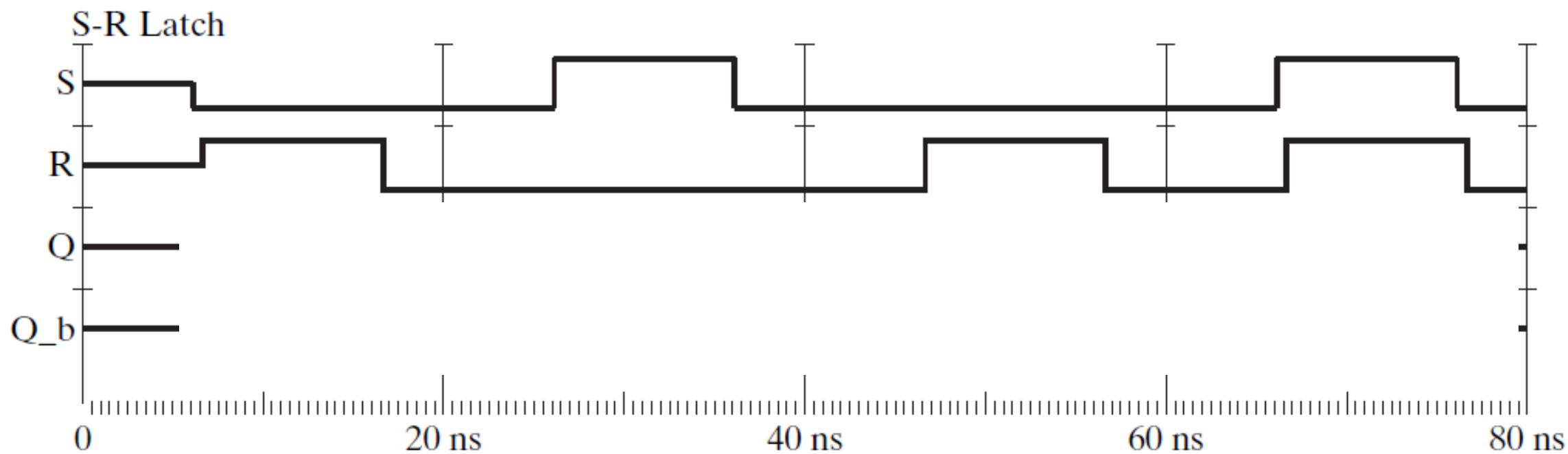


$$Q(t+\delta) = X(t)' \text{ and } X(t+\delta) = Q(t)'$$

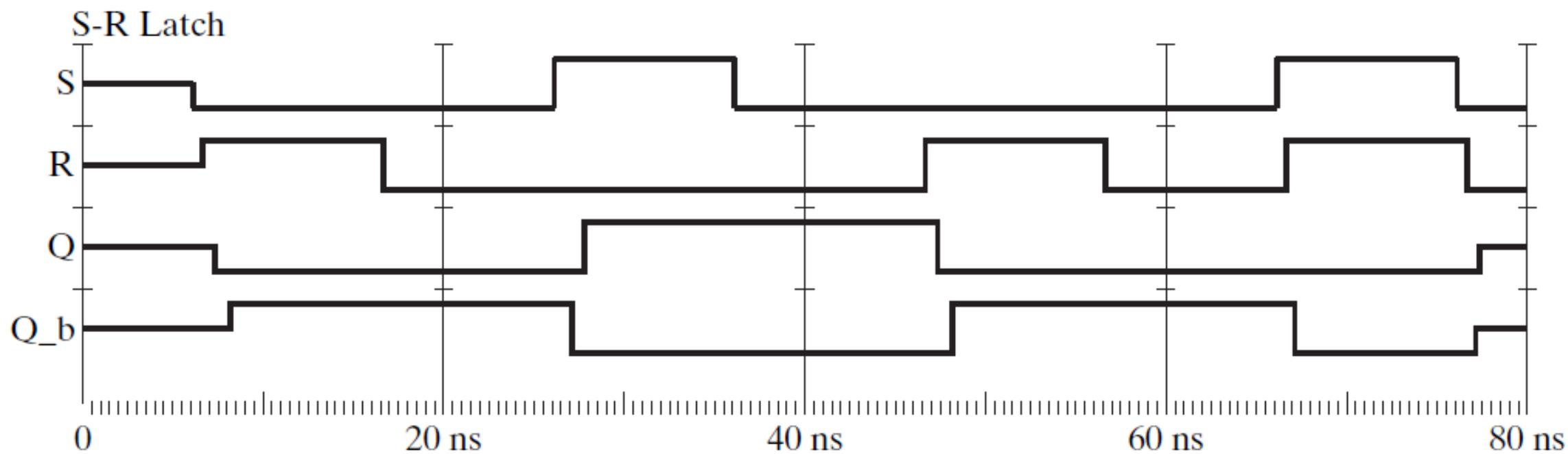


若SR存在同时由1到0的变化，存在延时 $\delta$ ，那么锁存器电路可能振荡

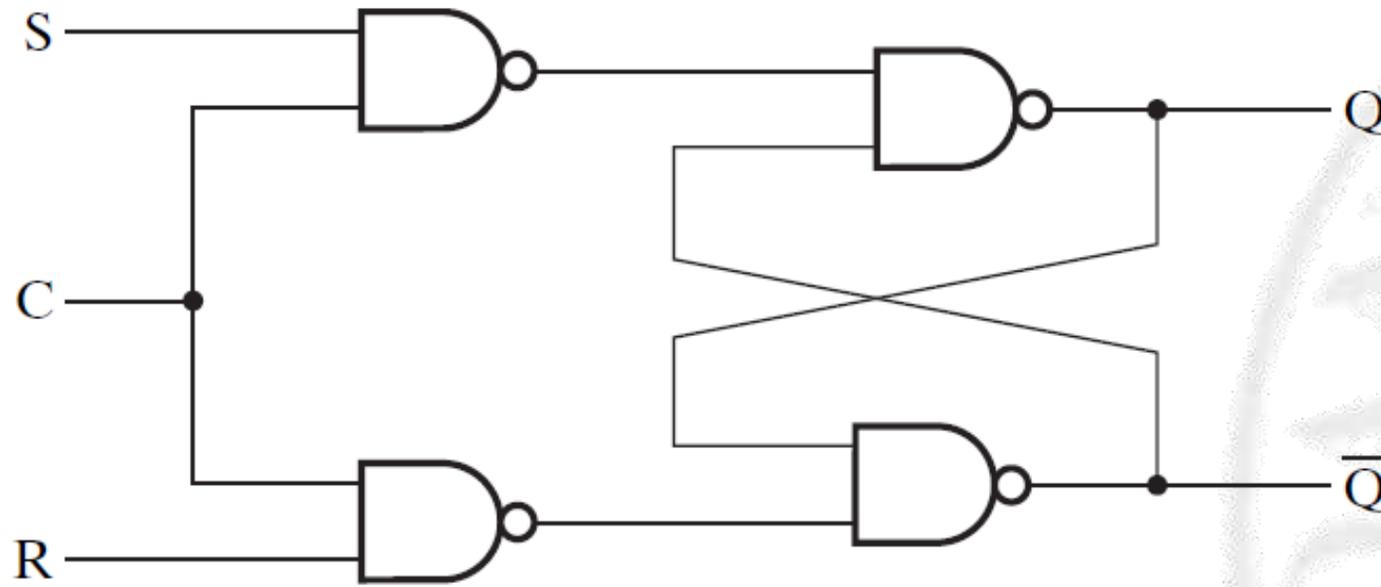
# SR 锁存器波形



# SR 锁存器波形



# 具有控制端的SR锁存器



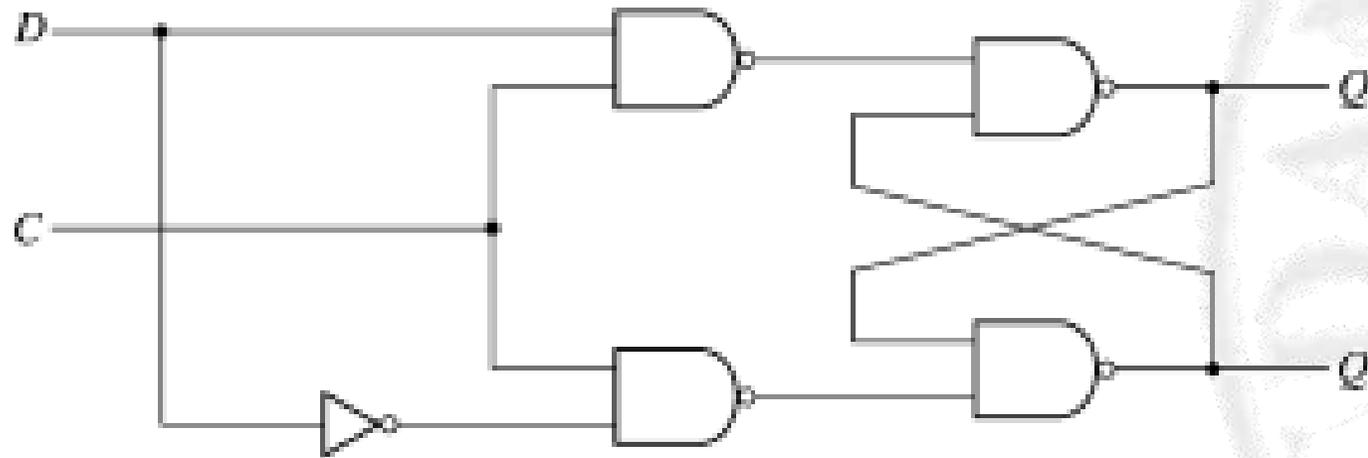
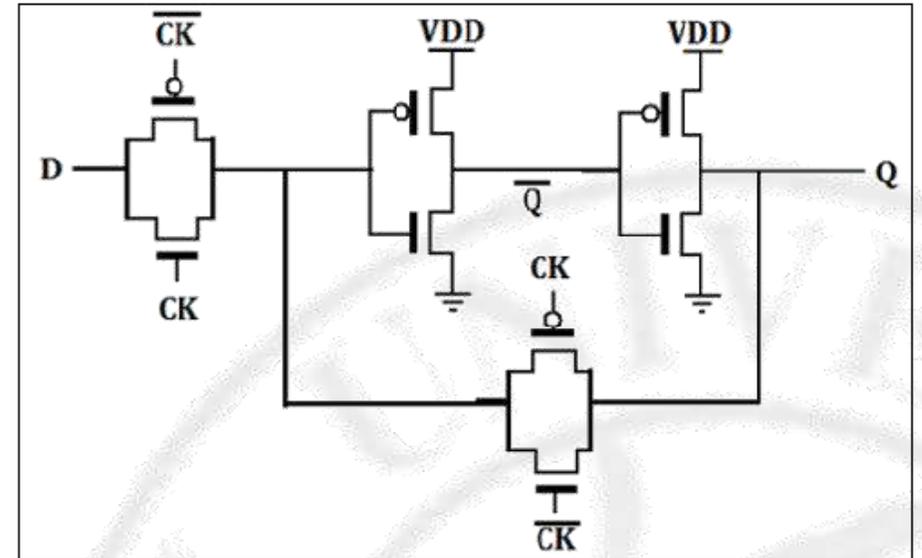
(a) Logic diagram

C	S	R	Next state of Q
0	X	X	No change
1	0	0	No change
1	0	1	Q = 0; Reset state
1	1	0	Q = 1; Set state
1	1	1	Undefined

(b) Function table

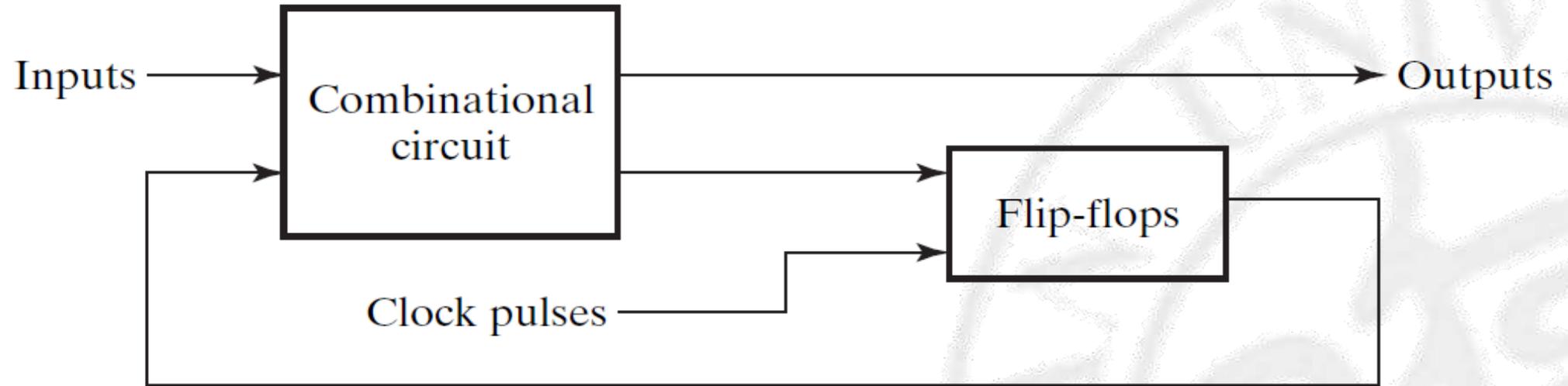
# D型锁存器

- D= Data
- 相比于输入端: 仅有数据输入, 和使能 (时钟输入)



$C$	$D$	Next state of $Q$
0	X	No change
1	0	$Q = 0$ ; Reset state
1	1	$Q = 1$ ; Set state

# 同步时序逻辑电路



(a) Block diagram



(b) Timing diagram of clock pulses